Exercise Sheet 3

winter term 2025/26

Discussion on 10.11.2025

Exercise 1. Check the conditions of Theorem 3.6 from the lecture for the following Runge-Kutta methods:

- Euler-Collatz method
- implicit trapezoidal method
- Heun method
- classical Runge-Kutta method

Exercise 2. Check the conditions of Theorem 3.7 from the lecture for the following Runge-Kutta methods:

- Euler-Collatz method
- implicit trapezoidal method
- Heun method
- classical Runge-Kutta method

Exercise 3. Determine the coefficients of the Adams-Bashforth-method for m=3.

- Exercise 4 (Programming exercise). 1. Implement the Euler-Collatz method and the implicit trapezoidal method. You can use the function fixpoint_iteration from ODE_solver.jl to solve the non-linear system of equations.
 - 2. Implement a routine that computes the ℓ^{∞} error of $(y_k)_{k=1,\dots,K}$ and $(y(t_k))_{k=1,\dots,K}$, if the exact solution is known.
 - 3. Compare the methods to the explicit Euler-method, the implicit Euler-method and the implicit midpoint method.