

**EXERCISES, Week 4** (submit by 07.11.2016)

1. Compute  $\int_{\gamma} (x + y) ds$ , where  $\gamma$  is the boundary of the triangle in  $\mathbb{R}^2$  with vertices at  $(0, 0)$ ,  $(1, 0)$ ,  $(0, 1)$ .
2. Compute  $\int_{\gamma} xy ds$ , where  $\gamma$  is the part of the circle  $x^2 + y^2 = 1$  located in the positive quadrant  $\{(x, y) \mid x \geq 0, y \geq 0\}$ .
3. Compute  $\int_{\gamma} z ds$ , where  $\gamma$  is the helix in  $\mathbb{R}^3$ ,  $\{(x, y, z) \mid x = t \cos t, y = t \sin t, z = t, 0 \leq t \leq 2\pi\}$ .
4. Compute  $\int_{\gamma} xy dx$ , where  $\gamma$  is the oriented curve  $\{(x, y) \mid y = \sin x, 0 \leq x \leq \pi\}$  with the orientation from  $x = 0$  to  $x = \pi$ .
5. Compute  $\int_{\gamma} 2xy dx + x^2 dy$ , where  $\gamma$  is the oriented curve  $\{(x, y) \mid y = \frac{x^2}{4}, 0 \leq x \leq 2\}$  with the orientation from  $x = 0$  to  $x = 2$ .
6. Compute  $\int_{\gamma} (y + z) dx + (z + x) dy + (x + y) dz$ , where  $\gamma$  is the oriented curve  $\{(x, y, z) \mid x = \sin^2 t, y = 2 \sin t \cos t, z = \cos^2 t, 0 \leq t \leq \pi\}$  with the orientation from  $t = 0$  to  $t = \pi$ .